

### **PART 1:**

If  $u = 0$ :

$$pA_1=0.4$$

$$pA_2=0.4$$

$$pA_3=0.4$$

$$pA_4=0.4$$

$$pA_5=0.4$$

$pA_t$  is constant.

If  $u = 0.4$ :

$$pA_1= 0.4458598726$$

$$pA_2= 0.4487392395$$

$$pA_3= 0.5281852561$$

$$pA_4= 0.5640610115$$

$$pA_5= 0.5964468487$$

From  $t = 0$ , to  $t=1$ ,  $pA_t$  is multiplied by a factor of roughly 1.114649682

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 1.006458009

From  $t = 2$ , to  $t=3$ ,  $pA_t$  is multiplied by a factor of roughly 1.177042722

From  $t = 3$ , to  $t=4$ ,  $pA_t$  is multiplied by a factor of roughly 1.067922675

From  $t = 4$ , to  $t=5$ ,  $pA_t$  is multiplied by a factor of roughly 1.006458009

Each time, it increases by a very little amount, but there isn't a direct relationship that can be defined numerically, as shows by the different factors each term is multiplied by to get to the next term.

If  $u = -0.4$ :

$$pA_1= 0.3225806452$$

$$pA_2= 0.2470119522$$

$$pA_3= 0.1792547371$$

$$pA_4= 0.1237022851$$

$$pA_5= 0.0818737159$$

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 0.806451613

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 0.7657370517

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 0.7256934461

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 0.6900921398

From  $t = 1$ , to  $t=2$ ,  $pA_t$  is multiplied by a factor of roughly 0.6618609821

## PART 2

The green line goes straight and remains on the line. This is because when  $u=0$ , the difference equation is:

$$\frac{pA_t(1 + 0)}{1 + 0 \times pA_t(2 - pA_t)}$$

Which then simplifies to:

$$\frac{pA_t}{1}$$

Which is equal to just  $pA_t$ , meaning that the value of  $pA_t$  will be constant.

When  $u = 0.4$ , it means that every organism with genotype AA, or AB will have, on average, 2.8 children. This is larger than 2, i.e., the number of organisms required to sexually reproduce, meaning that the overall population of the species is growing. The number of organisms with allele A will also be growing by the same amount as the total population growth, as it is their offspring that is making the population bigger. Therefore, we can express this as something like:

$$\frac{\text{population with allele A} + x}{\text{total population} + x}$$

Where  $x$  is the growth in the population. An increase in the numerator and an increase in the denominator by the same amount, there will be an increase on the overall fraction on the overall value.

However, when  $u = -0.4$ , the opposite is true, and can be expressed as something along the lines of this:

$$\frac{\text{population with allele} - x}{\text{total population} - x}$$

When you decrease both the numerator and the denominator by the same amount, there will be a decrease in the overall value of the fraction, however this decrease will be bigger than the increase than the increase when  $u=0.4$ , explaining why the red line approaches 0 quicker than the blue line approaches 1.  
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