

Competition 8: Evolution Puzzles

- ① Parent 1 = AB
Parent 2 = AB

	A	B
A	AA	BA
B	AB	BB

25% chance you inherit the disease

②

	A	A		B	B
A	AA	AA	A	BA	BA
B	AB	AB	B	BB	BB

50% disease	0% disease
50% carrier	50% carrier
0% none	50% none

↑
not possible
↳ AA cannot have children

20%, $\frac{1}{5}$ have gene

if both parents are carriers, $p(\text{child having disease}) = 25\%$
if one/both parents are BB, $p(\text{child having disease}) = 0\%$
if one/both parents are AA, $p(\text{child having disease}) = 0\%$

Conditions for child to have disease: ^{also}
- parents both AB / other parent is AB
- inherit A from both parents

$p(\text{other parent is AB}) = 20\% = \frac{1}{5}$
 $p(\text{inherit A from both}) = 25\% = \frac{1}{4}$

Since must have both $\frac{1}{5} \times \frac{1}{4} = \frac{1}{20}$

③

$$\frac{1}{5} \times \frac{1}{5} \times \frac{1}{4} = \frac{1}{100}$$

④ 50%

↳ offspring of AB with either AB or BB has a 50% chance of being a carrier

⑤ $p(\text{children are carriers}) = 50\%$
 $p(\text{grandchildren are carriers}) = \text{50\%} \cdot 25\%$

$$50\% \times 50\% = 25\%$$

$$\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

Answers:

- ① 25%
② $\frac{1}{20}$
③ $\frac{1}{100}$
④ 50%
⑤ 25%